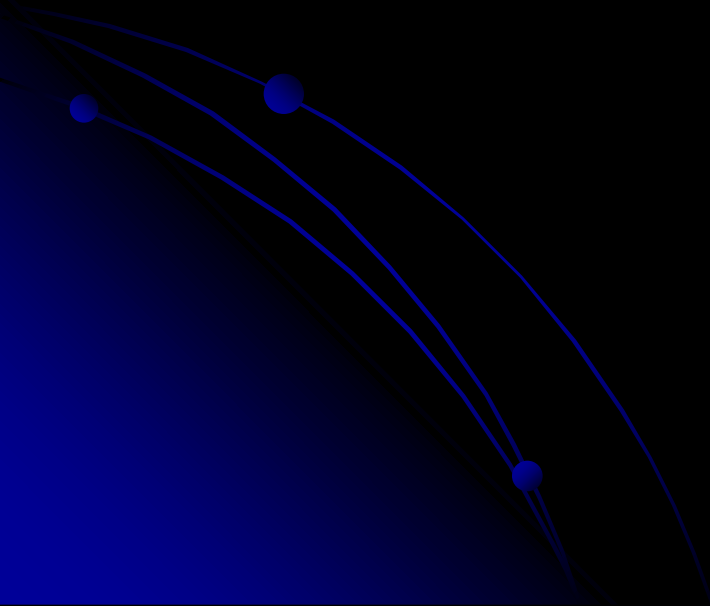




# Hľadanie hrán

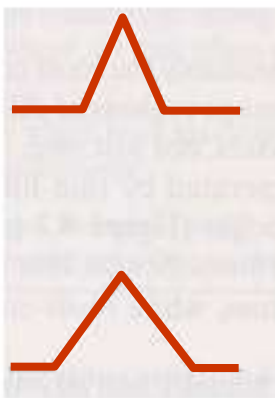


# Typy hrán

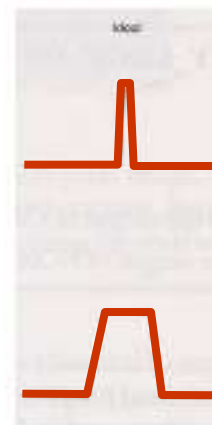
skutočné hrany -  
šum



schod  
rampa

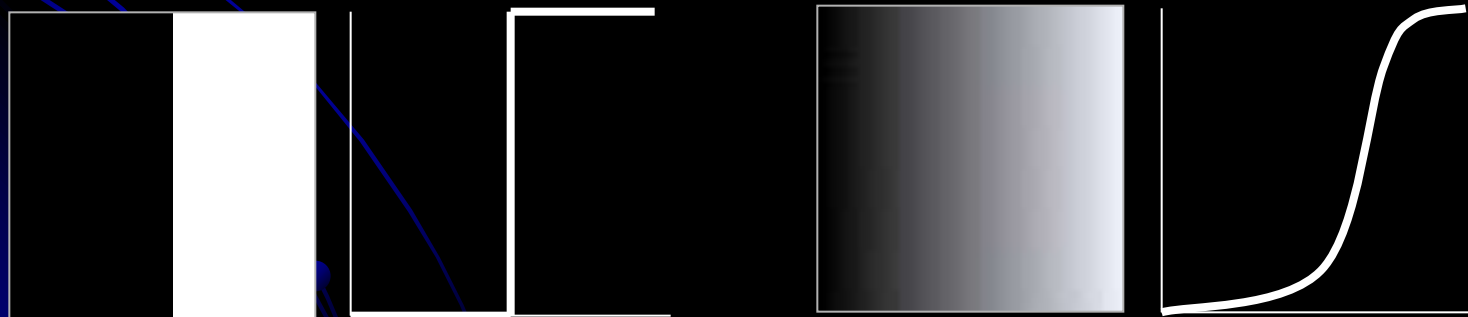
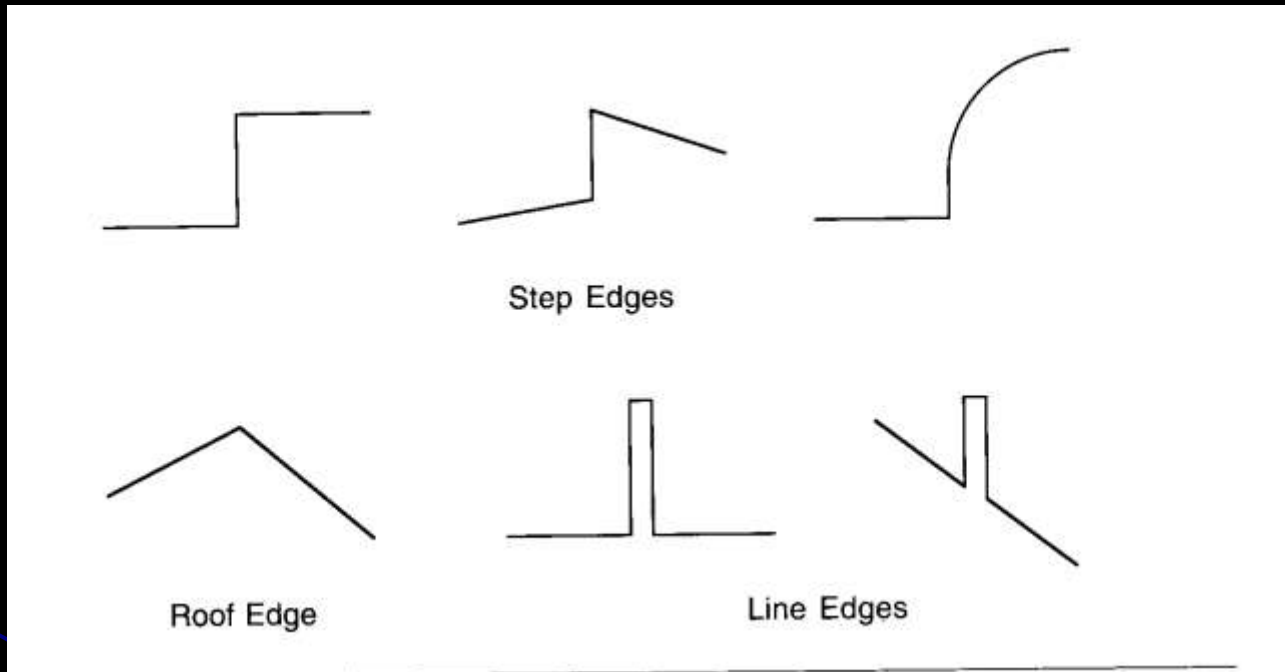


strecha



čiara  
hrebeň

# Typy hrán

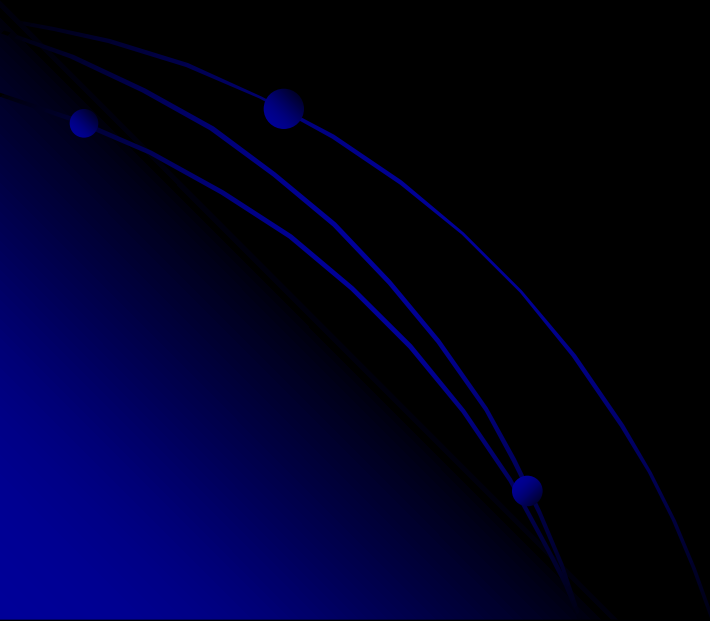


# Hľadanie hrán

skúmame body v okolí (pomocou **derivácie**)

Ak sa intenzity príliš nelíšia - pravdepodobne tam  
nie je hrana

Ak sa líšia - bod môže patriť hrane



# Metódy hľadania hrán

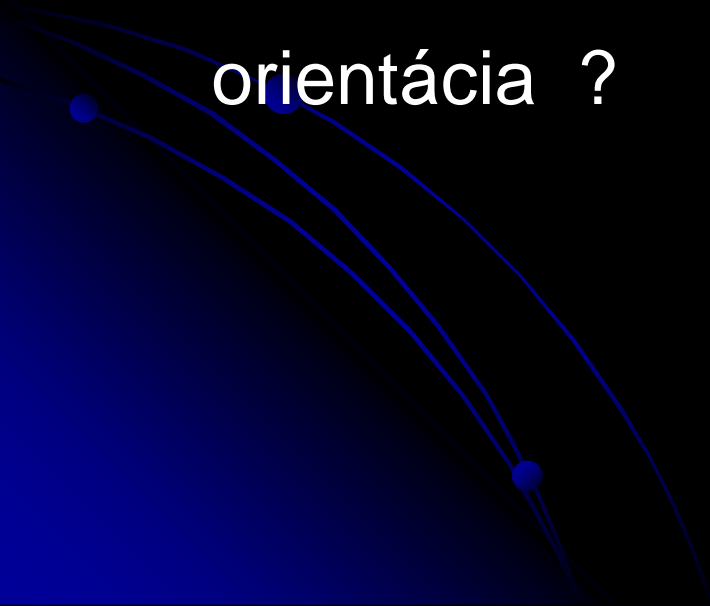
konvolučné masky

diskrétna aproximácia diferenciálnych operátorov  
(mera zmeny intenzity)

Informácia o:

existencia ✓

orientácia ?



# Diferencovanie 2D

$$\frac{\partial f(x, y)}{\partial x} \approx \frac{f(x_{n+1}, y_m) - f(x_n, y_m)}{\Delta x}$$

$$\frac{\partial f(x, y)}{\partial y} \approx \frac{f(x_n, y_{m+1}) - f(x_n, y_m)}{\Delta y}$$

$$\frac{\partial I(x, y)}{\partial x} = \frac{I(x+1, y) - I(x-1, y)}{2}$$

$$\frac{\partial I(x, y)}{\partial y} = \frac{I(x, y+1) - I(x, y-1)}{2}$$

$$\begin{bmatrix} 1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$\frac{\partial I}{\partial x} = I * \begin{bmatrix} 1 & 0 & -1 \end{bmatrix}$$

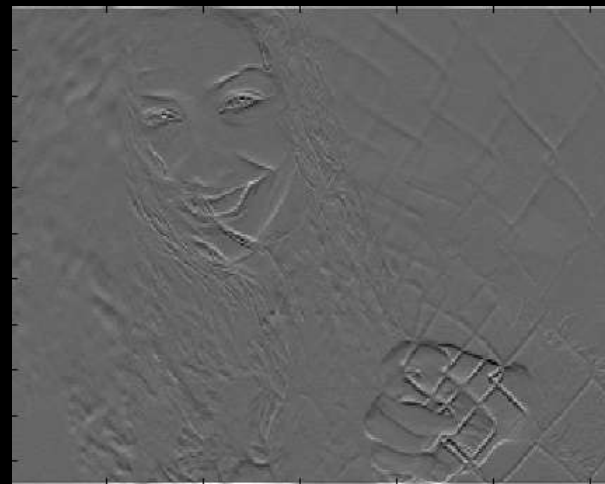
$$\frac{\partial I}{\partial y} = I * \begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix}$$

# Diferencovanie



$$I_x = I * \begin{bmatrix} 1 & -1 \end{bmatrix}$$

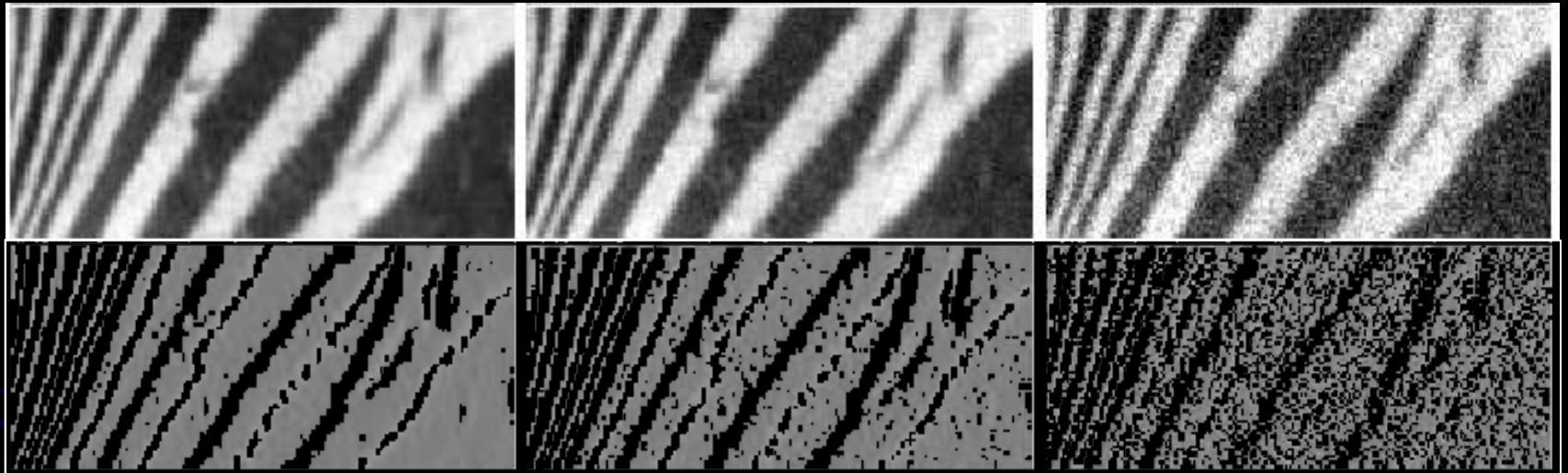
|



$$I_y = I * \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

Ktorý obrázok je  $I_x$ ?

# Diferencovanie a šum





# Vyhladenie

*prah 20*



*prah 50*

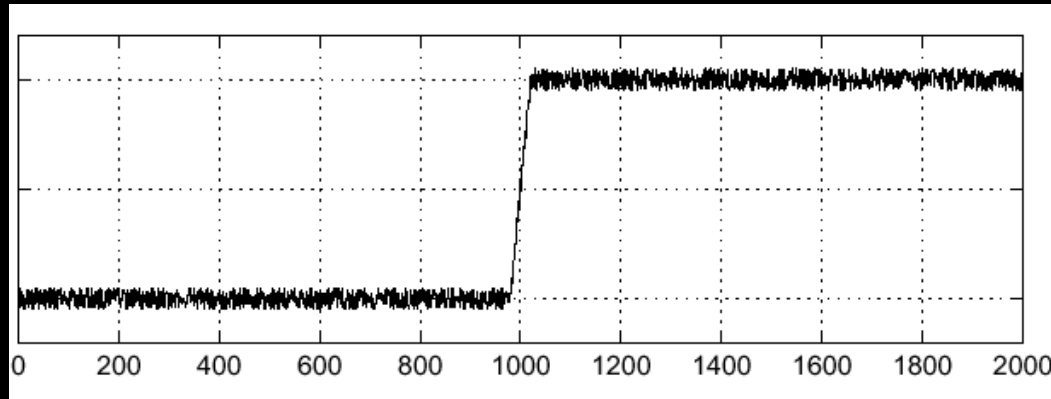


*originál*

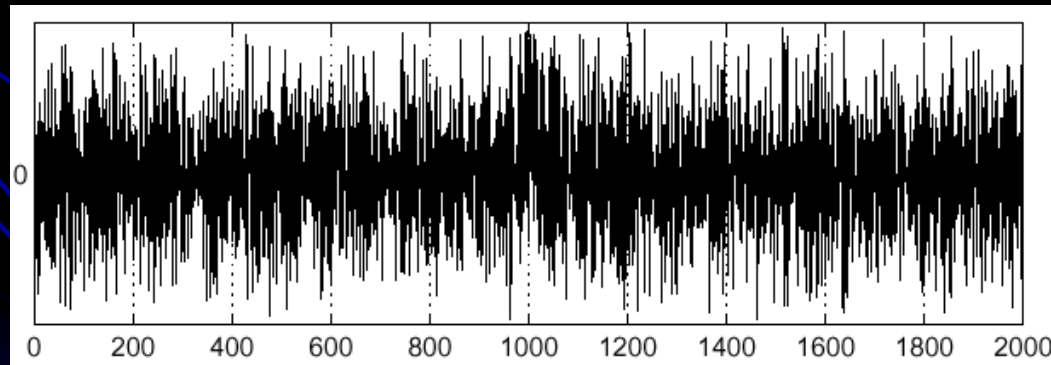
*Gaussovské vyhladenie*

# Následky šumu

$$f(x)$$

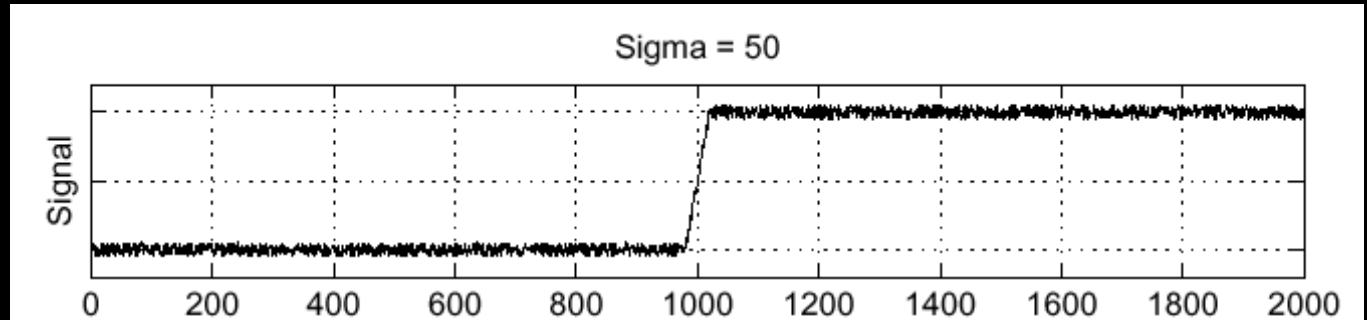


$$\frac{d}{dx} f(x)$$



# Vyhladenie

$f$



$h$

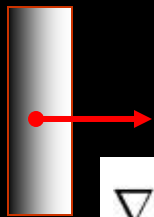
$h \star f$

$\frac{\partial}{\partial x}(h \star f)$

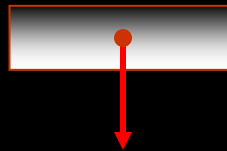
# Gradient

Gradient:  $\nabla f = \left[ \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$

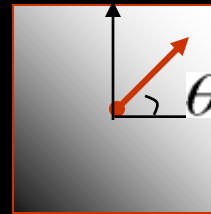
Smer – najväčšia zmena intenzity



$$\nabla f = \left[ \frac{\partial f}{\partial x}, 0 \right]$$



$$\nabla f = \left[ 0, \frac{\partial f}{\partial y} \right]$$



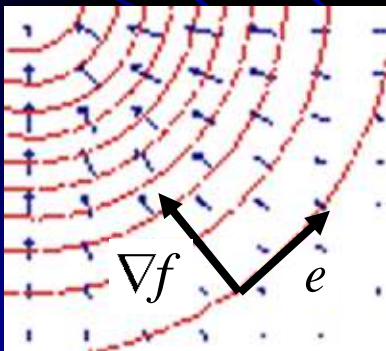
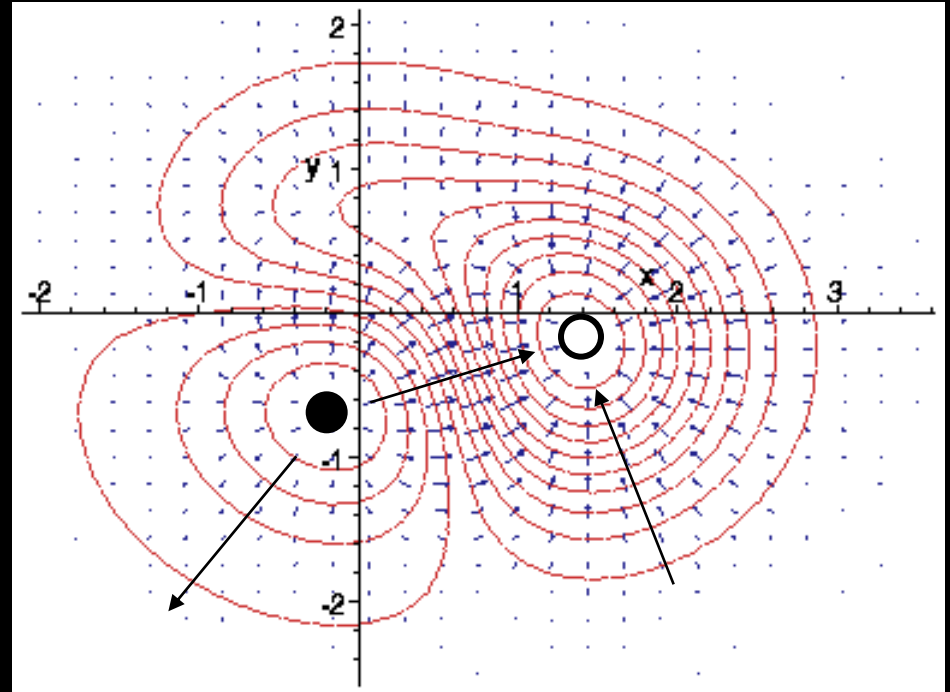
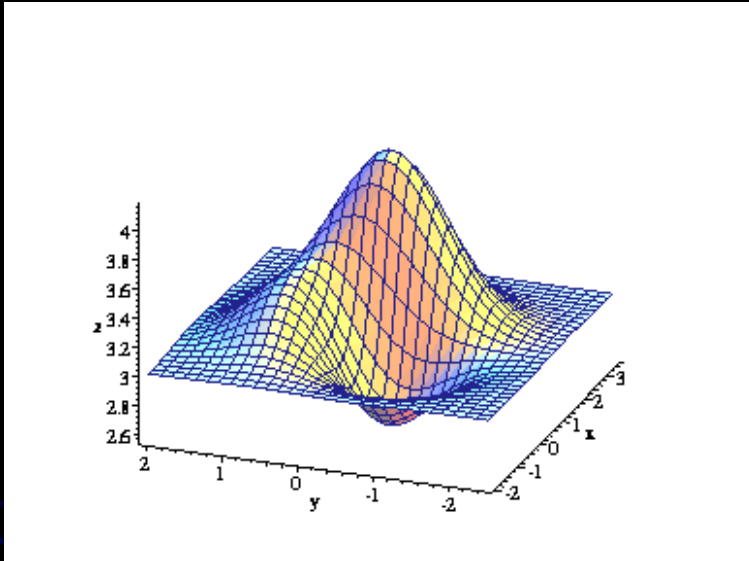
$$\nabla f = \left[ \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$$

Smer gradientu:  $\theta = \tan^{-1} \left( \frac{\partial f / \partial y}{\partial f / \partial x} \right)$

Veľkosť gradientu:  $\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$

$$\|\nabla f\| \approx |G_x| + |G_y|$$

# Gradient / hrany



Sila (dôležitosť) hrany = veľkosť gradientu  
Smer hrany = smer gradientu – 90

# Gradient



# Roberts

Najjednoduchšie masky

Len body hrán

Nie orientácia

Vhodné pre binárne obrázky

Nevýhody:

- Veľká citlivosť na šum

- Nepresná lokalizácia

- Málo bodov na aproximáciu gradientu

-1	0
0	1

0	-1
1	0

# Sobel

Hľadá horizontálne a vertikálne hrany

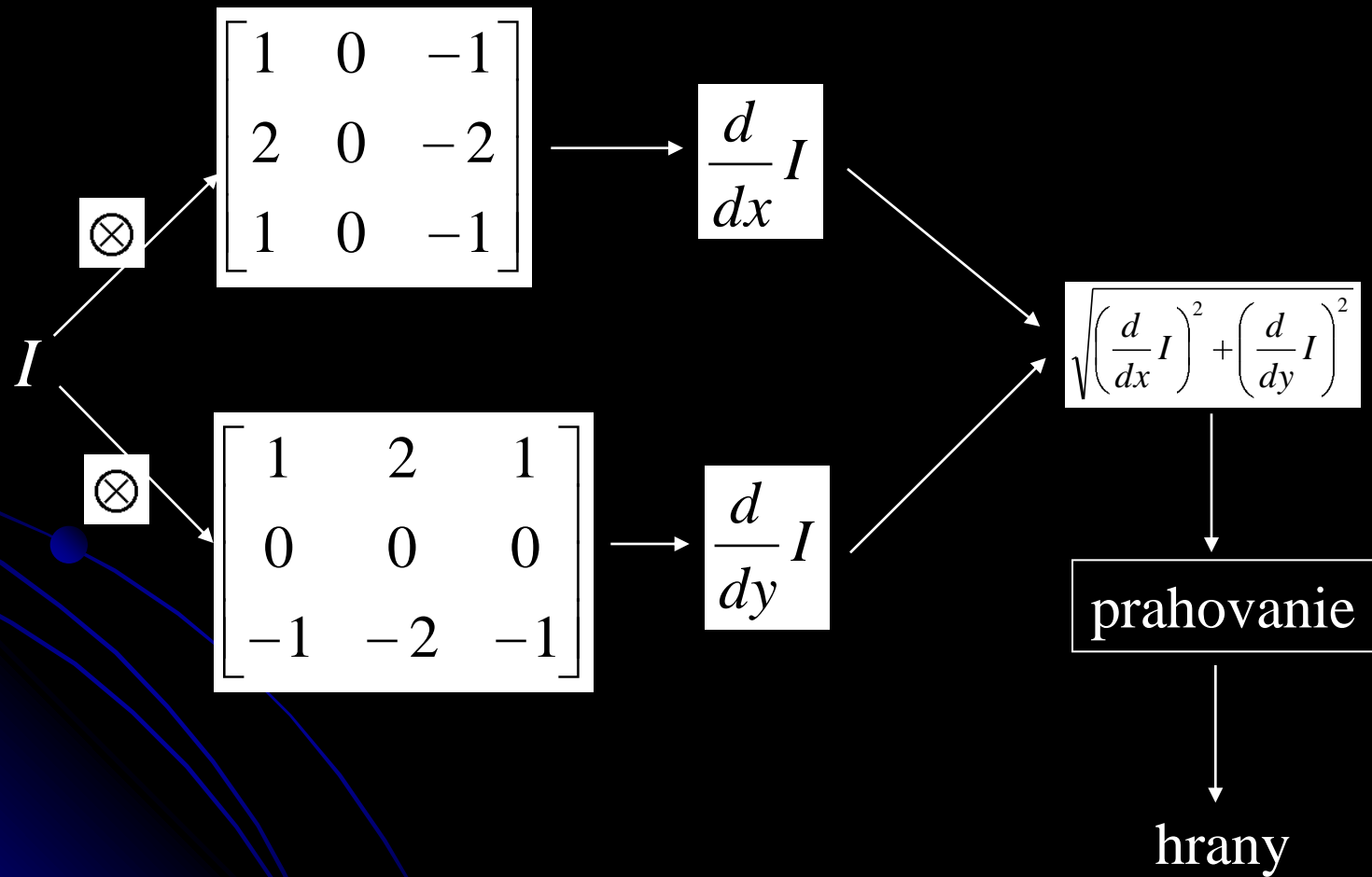
Konvolučné masky:

$$y = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

$$x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

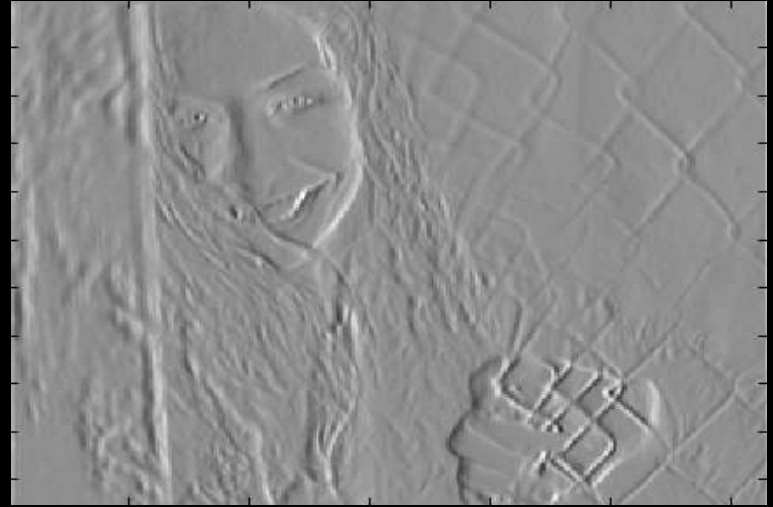


# Sobel

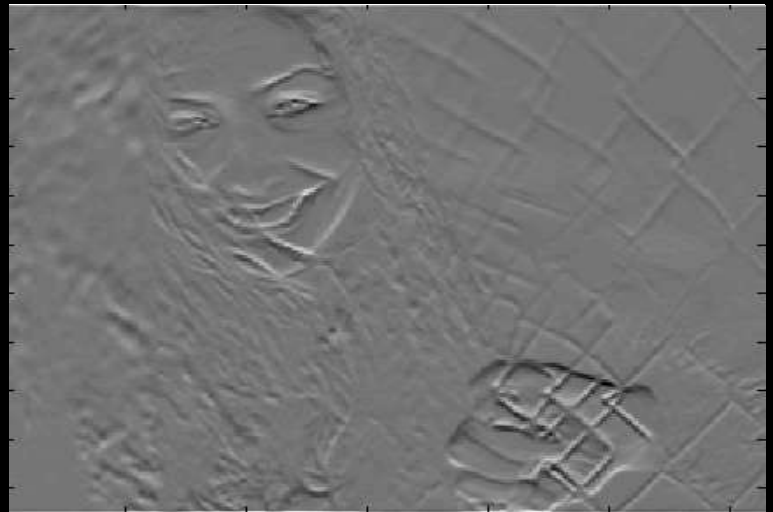


# Sobel

$$\frac{d}{dx} I$$



$$\frac{d}{dy} I$$

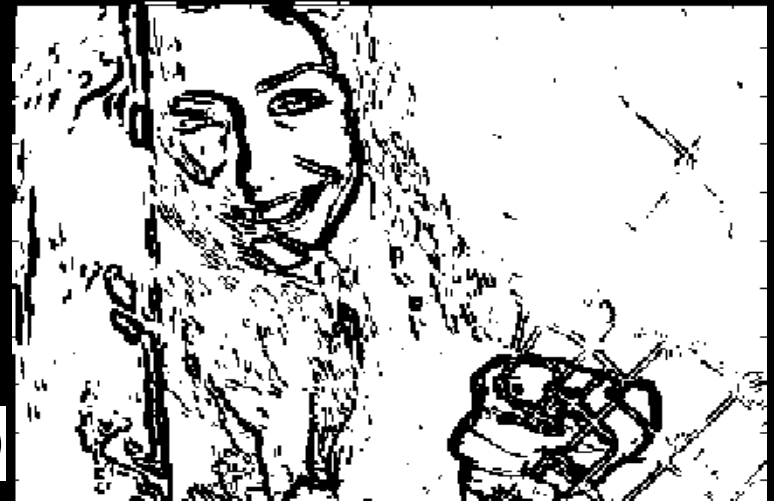


*I*



# Sobel

$$E = \sqrt{\left(\frac{d}{dx} I\right)^2 + \left(\frac{d}{dy} I\right)^2}$$



$E \geq \text{Threshold} = 100$

*I*



# Prewitt

Podobne ako Sobel

Masky:

$$y = \begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$x = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$$

# Prewitt

$$\frac{d}{dx} I$$



*I*



$$\frac{d}{dy} I$$



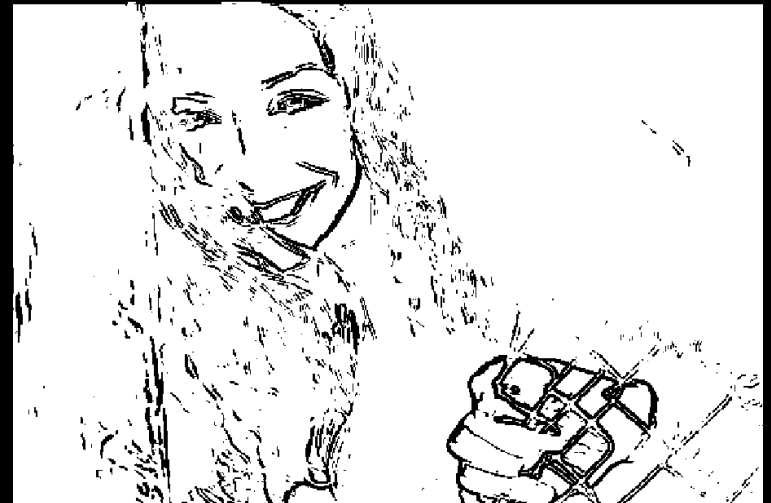
# Prewitt

$$E = \sqrt{\left(\frac{d}{dx} I\right)^2 + \left(\frac{d}{dy} I\right)^2}$$

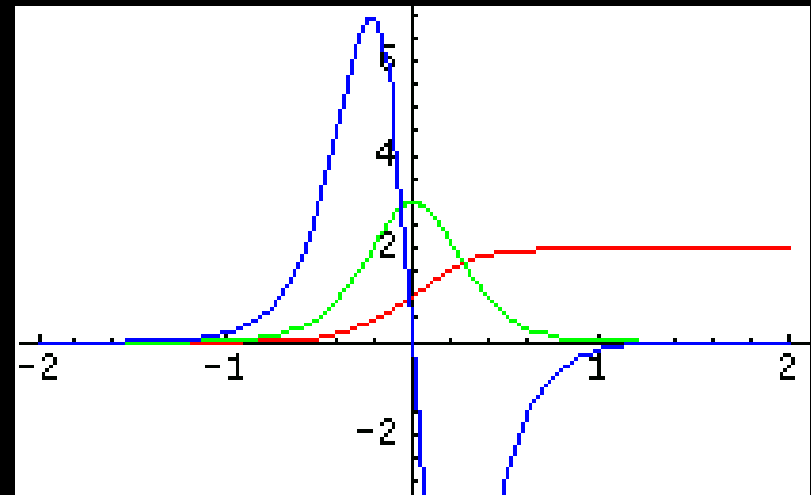
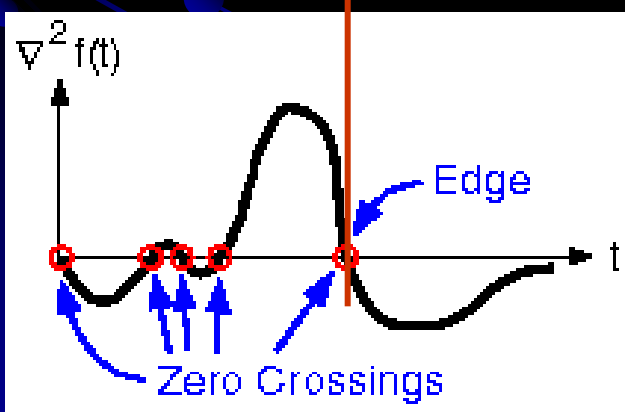
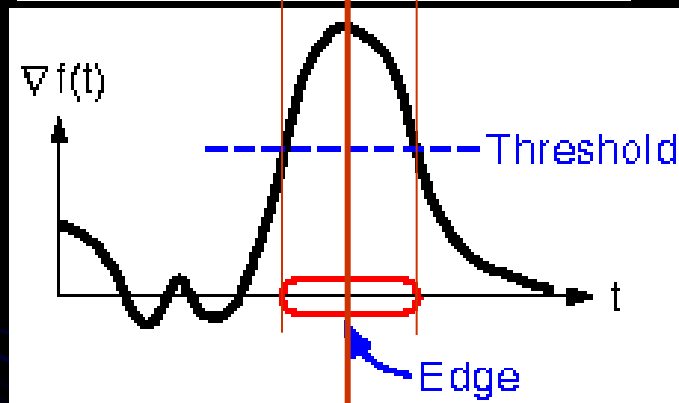
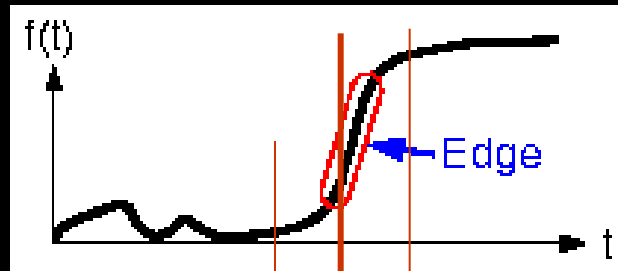
*I*



$E \geq 100$



# Druhá derivácia



# Laplacián

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

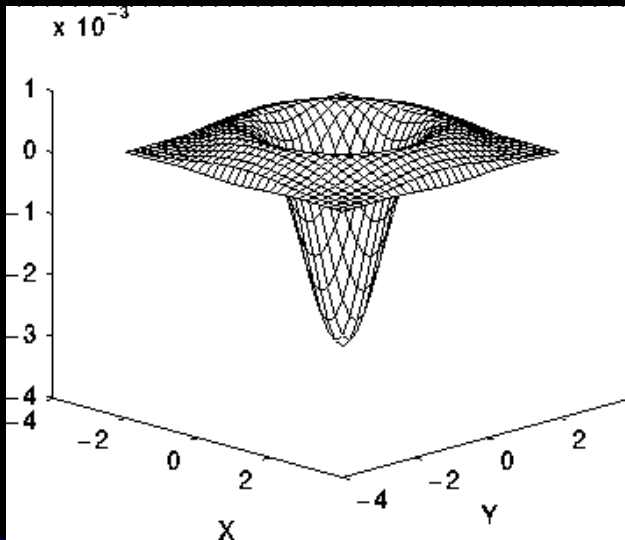
$$\frac{\partial^2 f}{\partial x^2} = f(i, j+1) - 2f(i, j) + f(i, j-1)$$

$$\frac{\partial^2 f}{\partial y^2} = f(i+1, j) - 2f(i, j) + f(i-1, j)$$

Konvolúcia [1, -2, 1]



# Laplacián



0	1	0
1	-4	1
0	1	0

1	1	1
1	-8	1
1	1	1

Nevýhody:

Velmi citlivý na šum

Produkuje dvojité hrany

Neurčuje smer hrany

# Laplacián



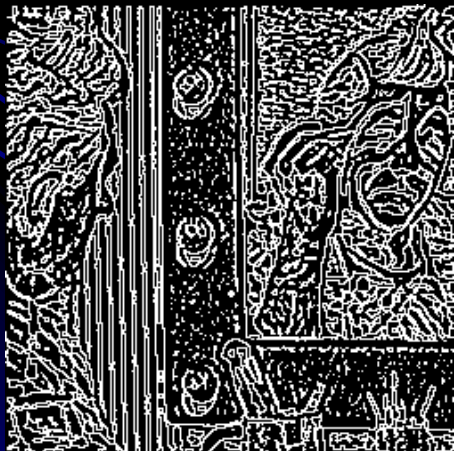
3×3



5×5



7×7



# Laplacián Gaussiánu

Marr – Hildreth operátor, LoG operátor

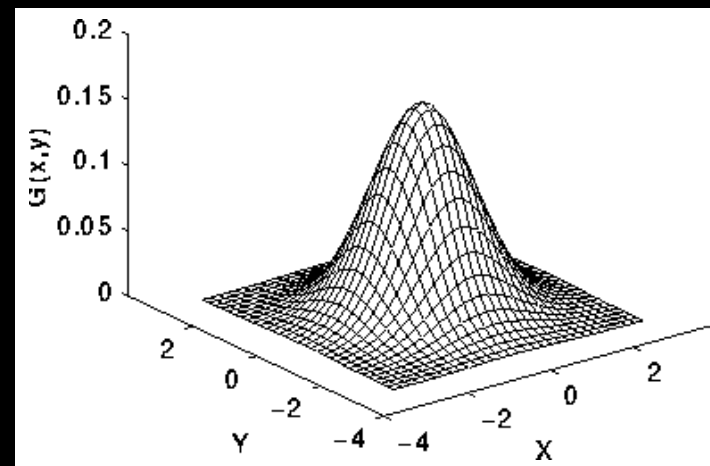
Vyhľadanie pomocou 2D Gaussiánu

$$S = G_{\sigma} \otimes I$$

Následná aplikácia Laplaciánu

$$\nabla^2 S = \frac{\partial^2}{\partial x^2} S + \frac{\partial^2}{\partial y^2} S$$

$$G_{\sigma} = \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

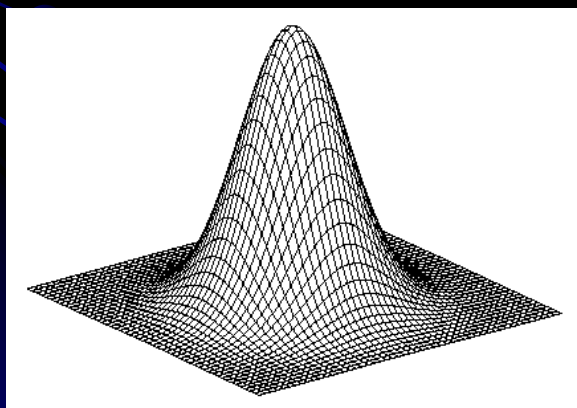


# Laplacián Gaussiánu

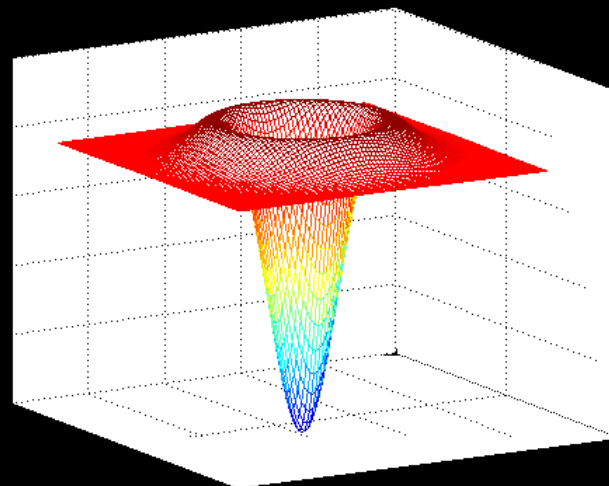
$$E = (I * G) * L = I * (G * L)$$

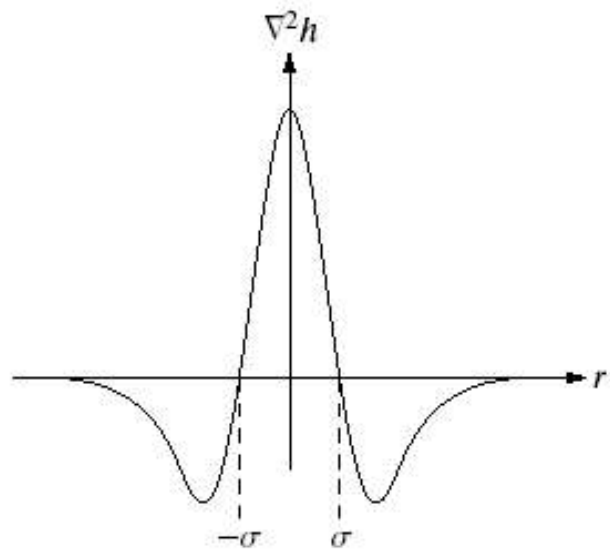
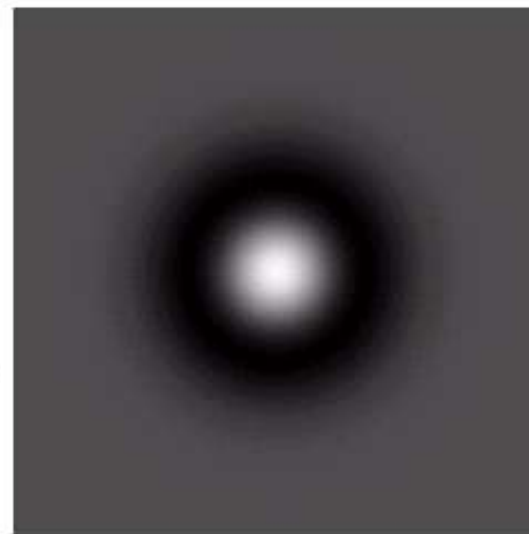
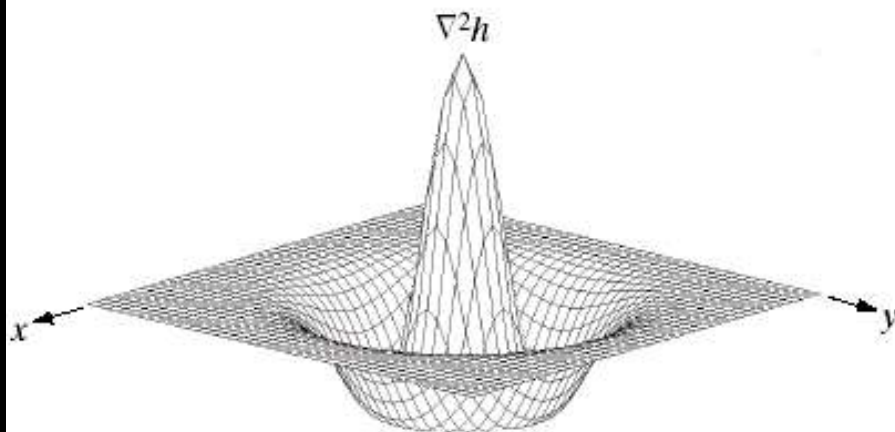
$$\nabla^2 S = \nabla^2 \mathbf{G}_\sigma * I \stackrel{\text{---}}{=} \nabla^2 \mathbf{G}_\sigma * I$$

Gaussian



Laplacian of Gaussian





0	0	-1	0	0
0	-1	-2	-1	0
-1	-2	16	-2	-1
0	-1	-2	-1	0
0	0	-1	0	0

a b  
c d

**FIGURE 10.14**  
Laplacian of a Gaussian (LoG).  
(a) 3-D plot.  
(b) Image (black is negative, gray is the zero plane, and white is positive).  
(c) Cross section showing zero crossings.  
(d)  $5 \times 5$  mask approximation to the shape of (a).

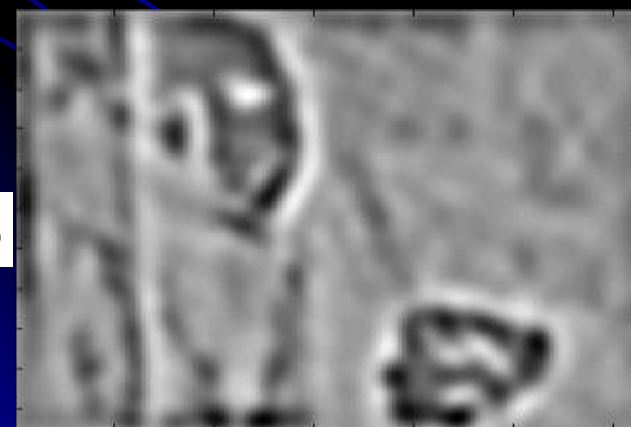
$\sigma = 1$



$\sigma = 3$



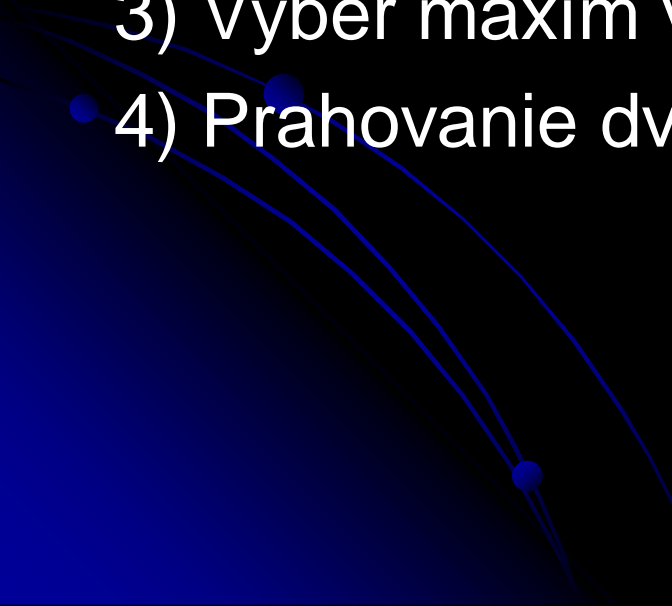
$\sigma = 6$



# Canny

1. Good detection – maximalizovať signal-to-noise pomer
2. Good localization – detekovaný bod hrany by mal byť čo najbližšie ku stredu skutočnej hrany
3. Only one response to a single edge

# Canny

- 1) Vyhladenie Gaussiánom
  - 2) Gradientný operátor
    - Veľkosť gradientu
    - Smer gradientu
  - 3) Výber maxím v danom smere
  - 4) Prahovanie dvoma prahmi
- 



Original



Canny



# Canny

Vyhladenie Gaussiánom  $S = G_\sigma * I$

Gradientný operátor (Sobel)

$$\nabla S = \left[ \frac{\partial}{\partial x} S \quad \frac{\partial}{\partial y} S \right]^T = \begin{bmatrix} S_x \\ S_y \end{bmatrix}^T$$

$$G_\sigma = \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

Veľkosť gradientu

$$|\nabla S| = \sqrt{S_x^2 + S_y^2}$$

Smer gradientu

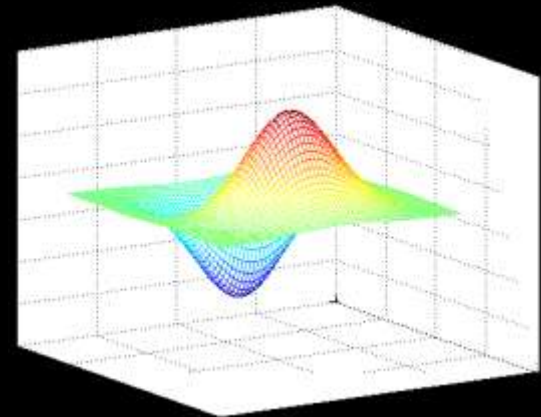
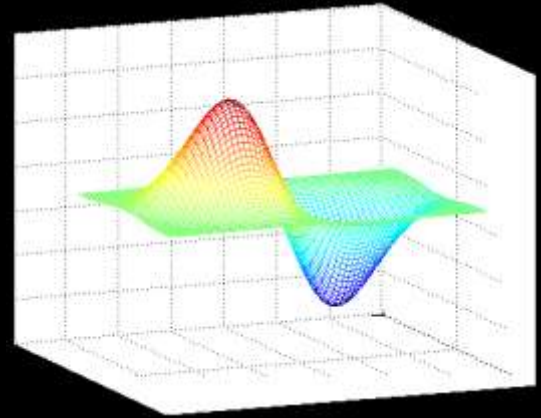
$$\theta = \tan^{-1} \frac{S_y}{S_x}$$

# Canny

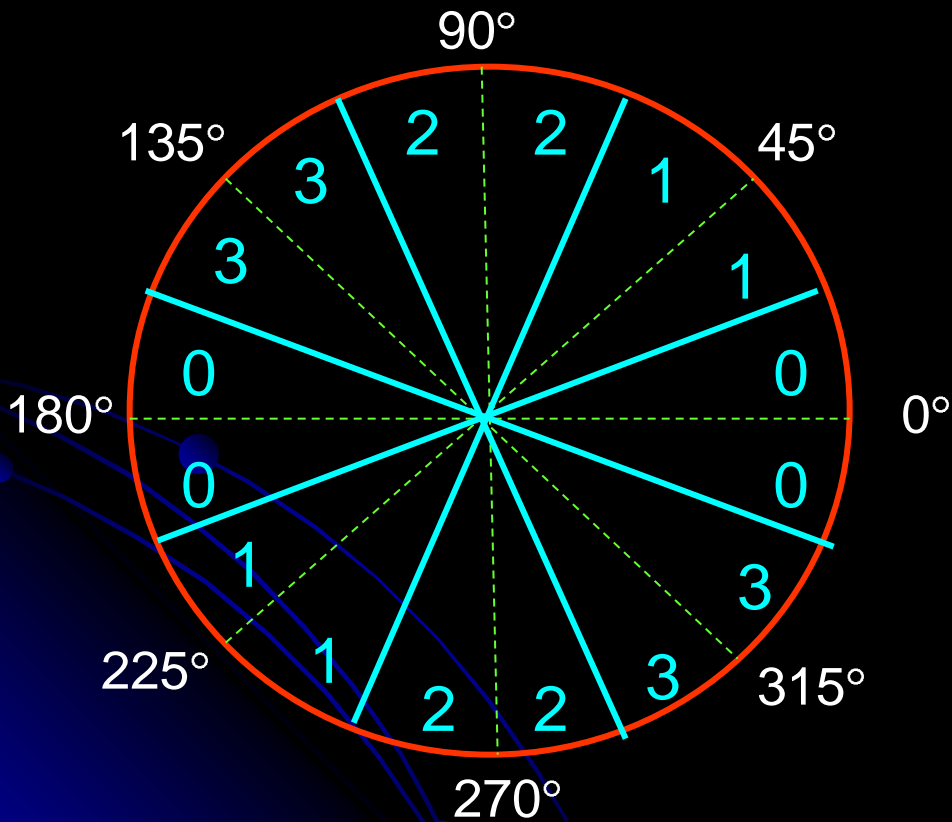
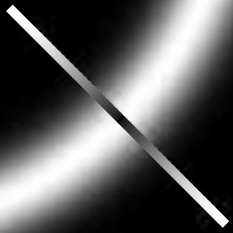
$$\nabla S = \nabla \mathbf{G}_\sigma * I \stackrel{-}{=} \nabla G_\sigma * I$$

$$\nabla G_\sigma = \begin{bmatrix} \frac{\partial G_\sigma}{\partial x} & \frac{\partial G_\sigma}{\partial y} \end{bmatrix}^T$$

$$\nabla S = \begin{bmatrix} \frac{\partial G_\sigma * I}{\partial x} & \frac{\partial G_\sigma * I}{\partial y} \end{bmatrix}^T$$



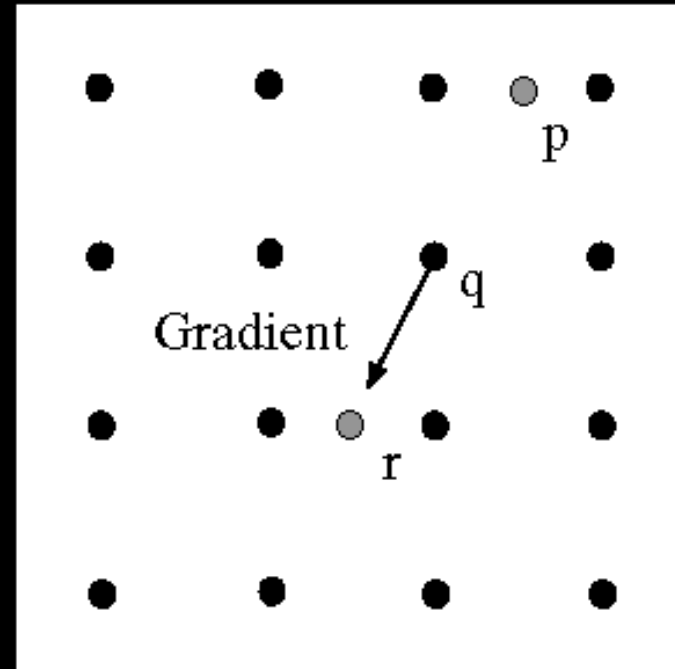
# Canny



$$M = |\nabla S|$$

$$\Theta$$

# Non-maximum suppression



Check if pixel is local maximum along gradient direction

requires checking interpolated pixels p and r

## Predicting the next edge point

Assume the marked point is an edge point. Then we construct the tangent to the edge curve (which is normal to the gradient at that point) and use this to predict the next points (here either  $r$  or  $s$ ).

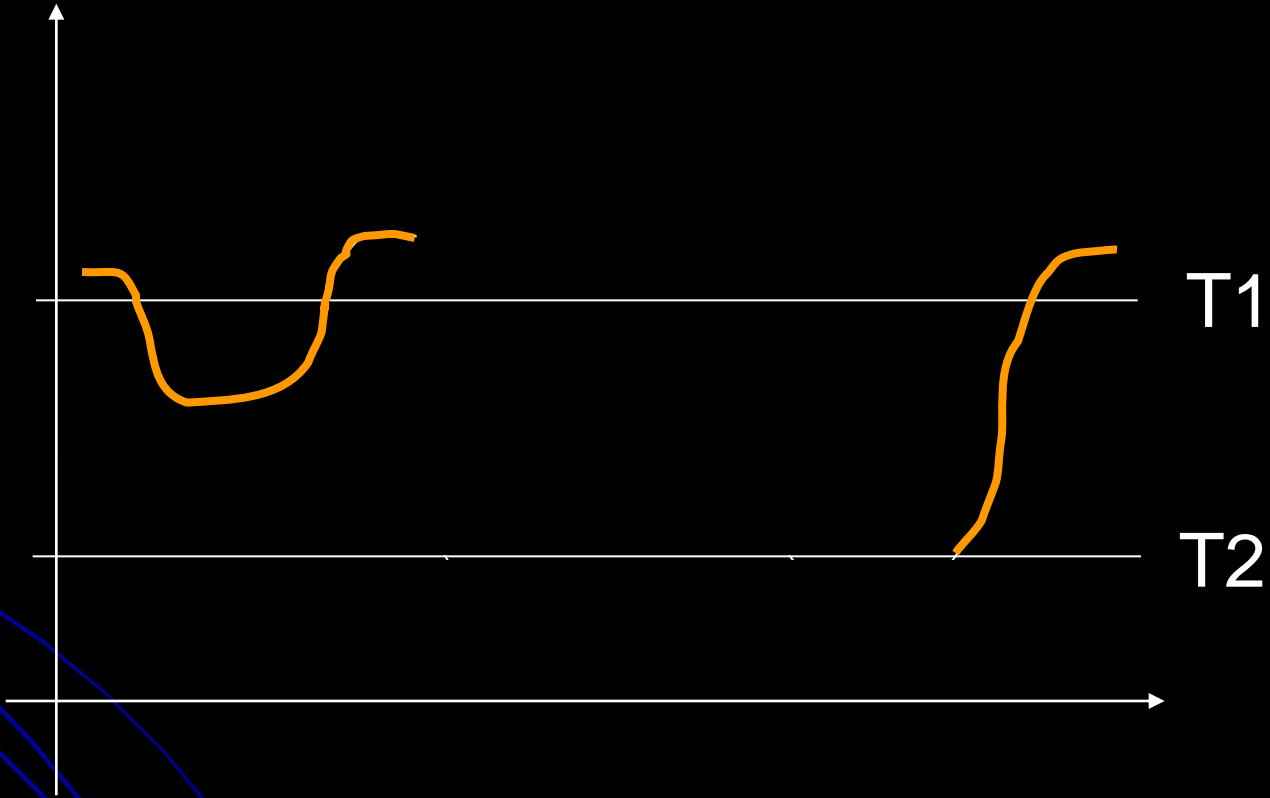


Gradient

(Forsyth & Ponce)

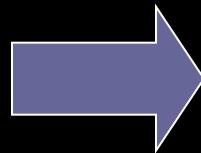


# Canny



# Canny príklady

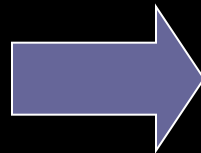
Gauss 5x5, T1=255, T2=1





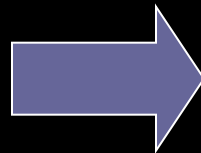
# Canny príklady

Gauss 5x5, T1=255, T2=220



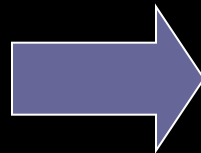
# Canny príklady

Gauss 5x5, T1=128, T2=1



# Canny príklady

Gauss 9x9, T1=128, T2=1





# Kirsch - kompas operátor

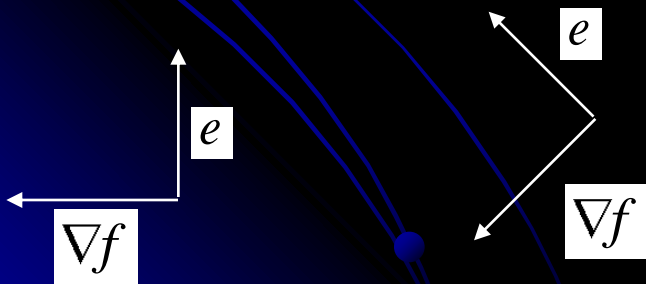
Rotujúca maska

Smery: 0 , 45 , 90 , 135 , ...

Sila hrany – maximum cez jednotlivé masky

Smer hrany – maska dávajúca maximum

$$\begin{bmatrix} -3 & -3 & 5 \\ -3 & 0 & 5 \\ -3 & -3 & 5 \end{bmatrix} \quad \begin{bmatrix} -3 & 5 & 5 \\ -3 & 0 & 5 \\ -3 & -3 & -3 \end{bmatrix} \quad \begin{bmatrix} 5 & 5 & 5 \\ -3 & 0 & -3 \\ -3 & -3 & -3 \end{bmatrix} \quad \begin{bmatrix} 5 & 5 & -3 \\ 5 & 0 & -3 \\ -3 & -3 & -3 \end{bmatrix} \quad \dots$$



# Robinson

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -2 & 1 \\ -1 & -1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -2 & -1 \\ 1 & -1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -1 \\ 1 & -2 & -1 \\ 1 & 1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & -1 & -1 \\ 1 & -2 & -1 \\ 1 & 1 & 1 \end{bmatrix}$$

Gradient  
direction

# Robinson Kirsch Prewitt

# Sobel

East  
 $H_1$

$$\begin{bmatrix} 1 & 1 & -1 \\ 1 & -2 & -1 \\ 1 & 1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 5 & -3 & -3 \\ 5 & 0 & -3 \\ 5 & -3 & -3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 0 & -1 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

Northeast  
 $H_2$

$$\begin{bmatrix} 1 & -1 & -1 \\ 1 & -2 & -1 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -3 & -3 & -3 \\ 5 & 0 & -3 \\ 5 & 5 & -3 \end{bmatrix}$$

$$\begin{bmatrix} 0 & -1 & -1 \\ 1 & 0 & -1 \\ 1 & 1 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & -1 & -2 \\ 1 & 0 & -1 \\ 2 & 1 & 0 \end{bmatrix}$$

North  
 $H_3$

$$\begin{bmatrix} -1 & -1 & -1 \\ 1 & -2 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -3 & -3 & -3 \\ -3 & 0 & -3 \\ 5 & 5 & 5 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

Northwest  
 $H_4$

$$\begin{bmatrix} -1 & -1 & 1 \\ -1 & -2 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -3 & -3 & -3 \\ -3 & 0 & 5 \\ -3 & 5 & 5 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -2 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix}$$

West  
 $H_5$

$$\begin{bmatrix} -1 & 1 & 1 \\ -1 & -2 & 1 \\ -1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -3 & -3 & 5 \\ -3 & 0 & 5 \\ -3 & -3 & 5 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

Southwest  
 $H_6$

$$\begin{bmatrix} 1 & 1 & 1 \\ -1 & -2 & 1 \\ -1 & -1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -3 & 5 & 5 \\ -3 & 0 & 5 \\ -3 & -3 & -3 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 1 \\ -1 & 0 & 1 \\ -1 & -1 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 2 \\ -1 & 0 & 1 \\ -2 & -1 & 0 \end{bmatrix}$$

South  
 $H_7$

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -2 & 1 \\ -1 & -1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 5 & 5 \\ -3 & 0 & -3 \\ -3 & -3 & -3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

Southeast  
 $H_8$

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -2 & -1 \\ 1 & -1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 5 & -3 \\ 5 & 0 & -3 \\ -3 & -3 & -3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 0 \\ 1 & 0 & -1 \\ 0 & -1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 1 & 0 \\ 1 & 0 & -1 \\ 0 & -1 & -2 \end{bmatrix}$$





# Farebné obrazy

Previest' na šedotónový a použiť niektorý z predchádzajúcich metód

**Problém** ak je hrana medzi dvomi farbami s rovnakým jasom

Vo farebnom obraze vieme určiť 90% hrán z šedotónového obrazu

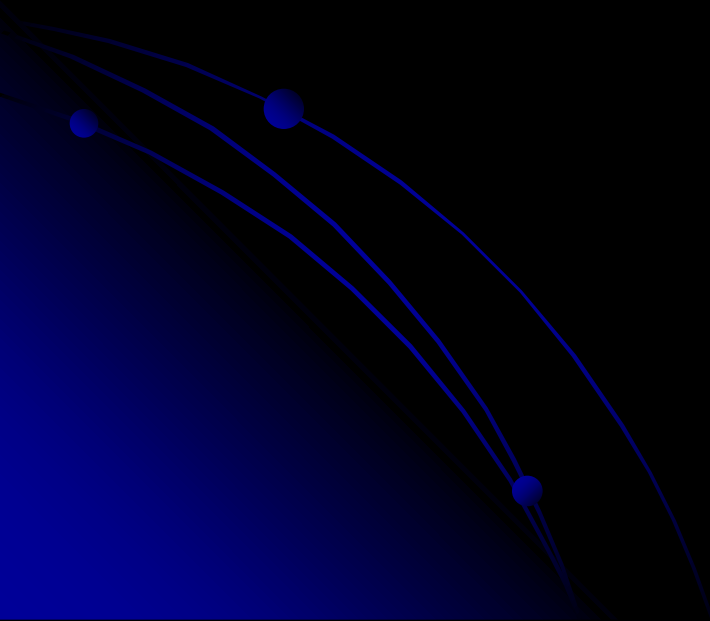
Zvyšných **10%** hrán z farebného obrazu

# Farebné obrázky

Sekvenčný prístup:

Jednotlivé kanály samostatne

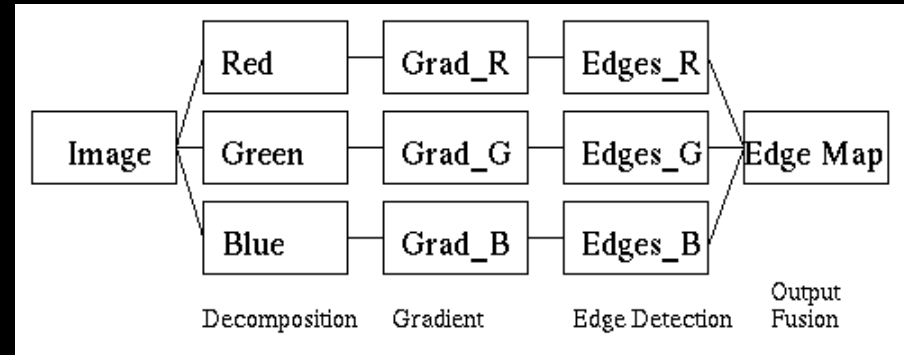
$$G(x, y) = \sqrt{G_{red}^2 + G_{green}^2 + G_{blue}^2}$$



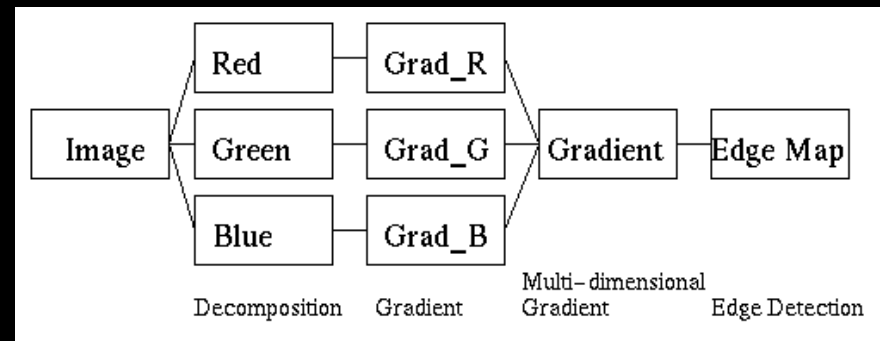


# Metódy

- output fusion methods



- multi-dimensional gradient methods



- vector methods

# Vektorový přístup

$$\mathbf{u} = (R'_x, G'_x, B'_x)$$

$$\mathbf{v} = (R'_y, G'_y, B'_y)$$

$$\mathbf{u} = \frac{\partial R}{\partial x} \mathbf{r} + \frac{\partial G}{\partial x} \mathbf{g} + \frac{\partial B}{\partial x} \mathbf{b}$$

$$\mathbf{v} = \frac{\partial R}{\partial y} \mathbf{r} + \frac{\partial G}{\partial y} \mathbf{g} + \frac{\partial B}{\partial y} \mathbf{b}$$

$$g_{xx} = \mathbf{u} \cdot \mathbf{u} = \mathbf{u}^T \mathbf{u} = \left| \frac{\partial R}{\partial x} \right|^2 + \left| \frac{\partial G}{\partial x} \right|^2 + \left| \frac{\partial B}{\partial x} \right|^2$$

$$g_{yy} = \mathbf{v} \cdot \mathbf{v} = \mathbf{v}^T \mathbf{v} = \left| \frac{\partial R}{\partial y} \right|^2 + \left| \frac{\partial G}{\partial y} \right|^2 + \left| \frac{\partial B}{\partial y} \right|^2$$

$$g_{xy} = \mathbf{u} \cdot \mathbf{v} = \mathbf{u}^T \mathbf{v} = \frac{\partial R}{\partial x} \frac{\partial R}{\partial y} + \frac{\partial G}{\partial x} \frac{\partial G}{\partial y} + \frac{\partial B}{\partial x} \frac{\partial B}{\partial y}$$

smer

$$\theta = \frac{1}{2} \tan^{-1} \left[ \frac{2g_{xy}}{(g_{xx} - g_{yy})} \right]$$

velikost'

$$F(\theta) = \sqrt{\frac{1}{2} \left[ (g_{xx} + g_{yy}) - (g_{xx} - g_{yy}) \cos(2\theta) + 2g_{xy} \sin(2\theta) \right]}$$

# Vector order statistics

- Používa sa R-ordering
- Okno  $W$  veľkosti  $n$  pixelov
- **Vector range (VR) edge detector** – najjednoduchší

$$VR = D(\mathbf{x}^{(n)}, \mathbf{x}^{(1)})$$

$\mathbf{x}^{(1)}$  – median ,  $\mathbf{x}^{(n)}$  - outlier

citlivý na šum

- **Vector dispersion edge detectors (VDED)**

$$VDED = \left\| \sum_{i=1}^n \alpha_i \mathbf{X}^{(i)} \right\|$$

$\alpha_i$  váhy

VR špeciálny prípad VDED kde  $\alpha_{(1)} = -1$  a  $\alpha_{(n)} = 1$ ,  $\alpha_{(i)} = 0$   
 $i = 2, \dots, n-1$



Fig. 4. Test image 'Lena'



Fig. 5. Test image 'Lena' distorted with the Gaussian and impulsive noises

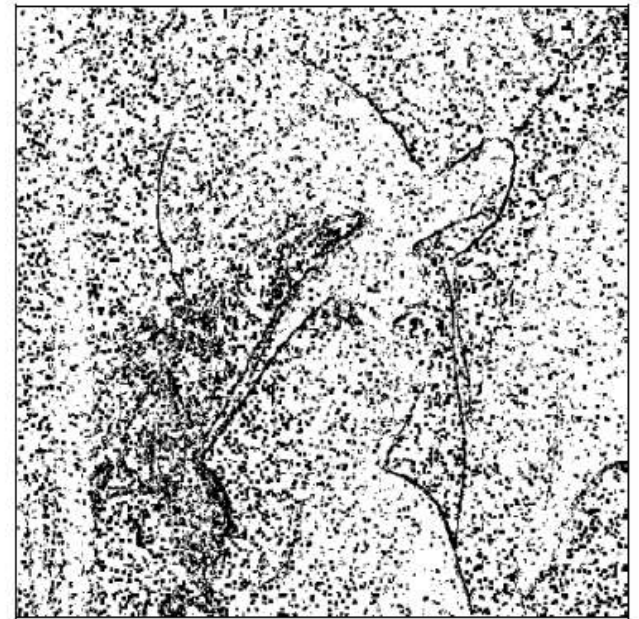


Fig. 6. VR detector: edges of the noised image 'Lena'

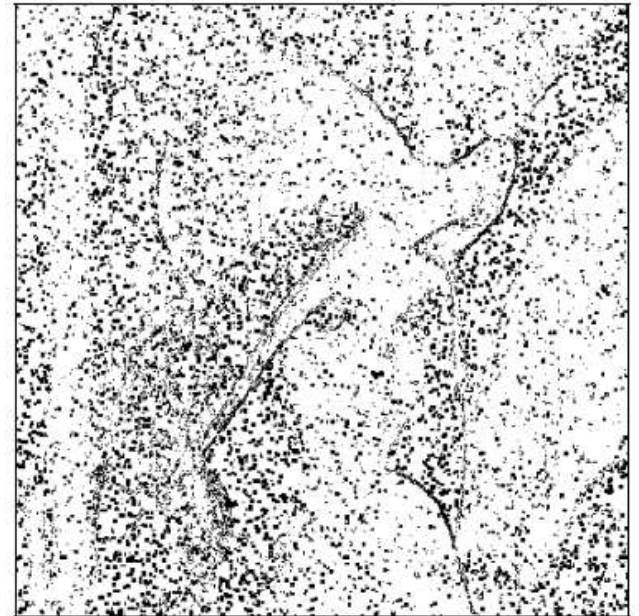


Fig. 7. VDED detector: edges of the noised image 'Lena'

## ***Minimum vector range***

Uvažujeme k rozdielov – odstránime citlivosť na šum (impulsive, exponential noise)

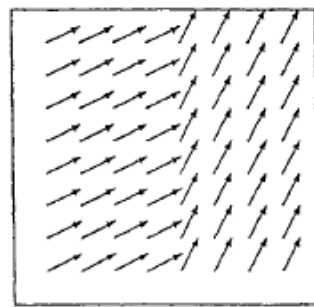
$$MVR = \min_j \left\{ \left\| \mathbf{X}^{(n-j+1)} - \mathbf{X}^{(1)} \right\| \right\},$$
$$j = 1, 2, \dots, k, k < n$$

***Minimum vector dispersion*** – odstráni citlivosť aj na Gaussov šum

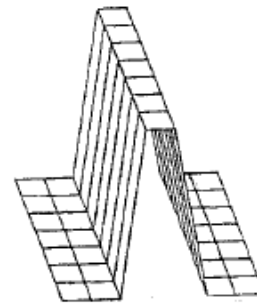
$$MVD = \min_j \left\{ \left\| \mathbf{X}^{(n-j+1)} - \sum_{i=1}^l \frac{\mathbf{X}^{(i)}}{l} \right\| \right\},$$
$$j = 1, 2, \dots, k, k, l < n$$

Používa  $\alpha$ -trimmed mean

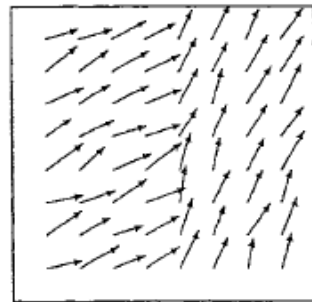




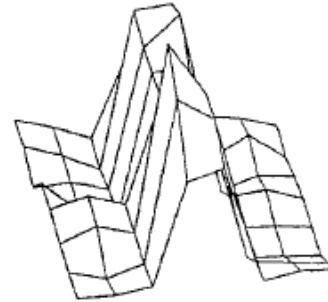
(a)



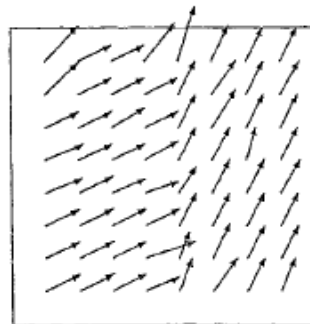
(b)



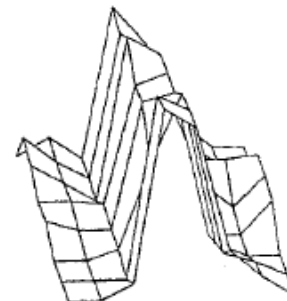
(c)



(d)



(e)



(f)

Fig. 4. Response of *MVD* to noise contaminated edge. (a) Initial edge, (b) Response of *MVD* to (a), (c) edge (a) corrupted with gaussian noise, (d) response of *MVD* to (c), (e) edge (a) corrupted with double-exponential noise, (f) response of *MVD* to (e).

## Nearest neighbour vector range

$$\text{NNVR} = D \left[ \mathbf{x}^{(n)}, \sum_{i=1}^n w_i \mathbf{x}^{(i)} \right]$$

$$w_i \geq 0$$

$$\sum_{i=1}^n w_i = 1$$

$$w_i = \frac{d^{(n)} - d^{(i)}}{n \cdot d^{(n)} - \sum_{j=1}^n d^{(j)}}$$

$$d_i = \sum_{j=1}^n D(\mathbf{x}_i, \mathbf{x}_j), \quad i = 1, 2, \dots, n$$

Nemôže byť použité na homogénne oblasti

- Kombináciou MVD a NNVR

$$\text{NNMVD} = \min_j \left\{ D \left[ \mathbf{x}^{(n-j+1)} \mid \sum_{i=1}^n w_i \mathbf{x}^{(i)} \right] \right\}$$

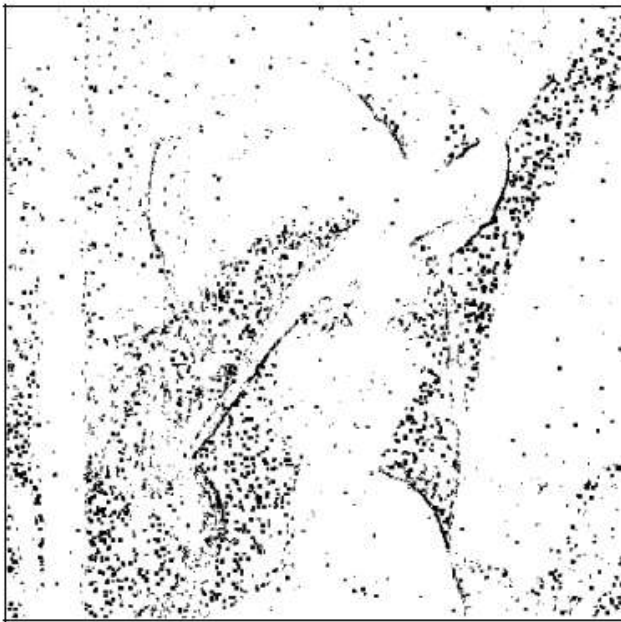


Fig. 8. NNVR detector: edges of the noised image 'Lena'



Fig. 9. MVD detector: edges of the noised image 'Lena'



Fig. 10. NNMVD detector: edges of the noised image 'Lena'

# Difference vector operators

Každý pixel reprezentovaný ako vektor v RGB

Vypočítame gradient v 4 smeroch

$$|\nabla f|_{0^\circ} = \|Y_{0^\circ} - X_{0^\circ}\|$$

$$|\nabla f|_{90^\circ} = \|Y_{90^\circ} - X_{90^\circ}\|$$

$$|\nabla f|_{45^\circ} = \|Y_{45^\circ} - X_{45^\circ}\|$$

$$|\nabla f|_{135^\circ} = \|Y_{135^\circ} - X_{135^\circ}\|$$

$$DV = \max(|\nabla f|_{0^\circ}, |\nabla f|_{45^\circ}, |\nabla f|_{90^\circ}, |\nabla f|_{135^\circ})$$



Fig. 11. DV detector: edges of the noised image 'Lena'

**X, Y sú 3D vektorové konvolučné masky**

# Základná maska pre okno 3x3

$v(x,y)$  – pixel,  $v(x_0,y_0)$  - stredný pixel

$$X_{0^\circ} = v(x_{-1}, y_0), \quad Y_{0^\circ} = v(x_1, y_0)$$

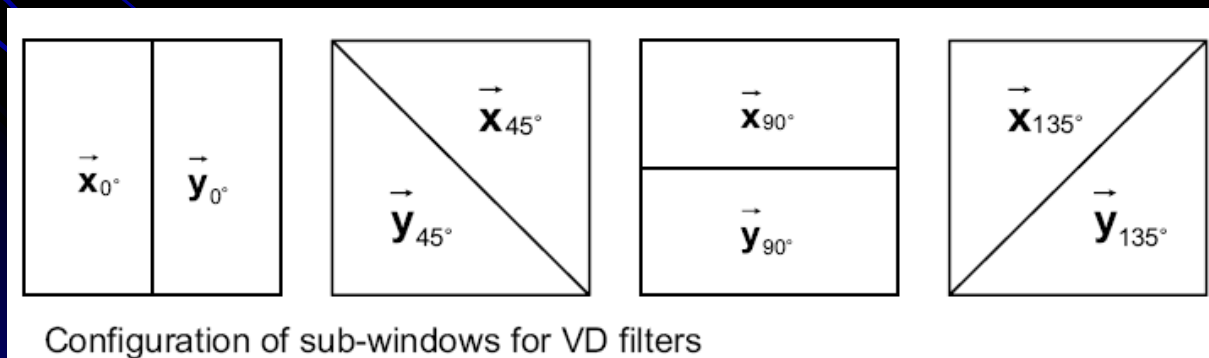
$$X_{45^\circ} = v(x_{-1}, y_1), \quad Y_{45^\circ} = v(x_1, y_{-1})$$

$$X_{90^\circ} = v(x_0, y_1), \quad Y_{90^\circ} = v(x_0, y_{-1})$$

$$X_{135^\circ} = v(x_1, y_1), \quad Y_{135^\circ} = v(x_{-1}, y_{-1})$$

Pred detekciou môžeme obraz filtrovať – treba použiť väčšiu masku

Ak okno  $W$  je veľkosti  $n \times n$  ( $n=2k+1$ ) vytvoríme sub-okno veľkosti  $N = (n^2-1)/2$



$$X_d = f(v_{d,1}^{sub_1}, v_{d,2}^{sub_1}, \dots, v_{d,N}^{sub_1})$$

$$Y_d = f(v_{d,1}^{sub_2}, v_{d,2}^{sub_2}, \dots, v_{d,N}^{sub_2})$$

where:  $d = 0^\circ, 45^\circ, 90^\circ, 135^\circ$ .

Podľa typu šumu môžeme použiť rôzne filtre

***Vector median filter***

$$f_{VM}(v_1, v_2, \dots, v_N) = v^{(1)}$$

- Efektívny pri redukovaní impulsného šumu

***Vector mean filter***

$$f_{VM}(v_1, v_2, \dots, v_N) = \frac{1}{N} \sum_{i=1}^N v_i$$

Efektívny pri redukovaní Gaussovho šumu

# Kombináciou predchádzajúcich

## *$\alpha$ -trimmed mean filter*

$$f_{\alpha\text{-trim}}(v_1, v_2, \dots, v_N) = \frac{1}{N(1-2\alpha)} \sum_{i=1}^{N(1-2\alpha)} v^{(i)}$$

where:  $\alpha$  is within  $[0, 0,5)$  interval.

## *Adaptive nearest neighbour filter*

$$f_{\text{adap}}(v_1, v_2, \dots, v_N) = \sum_{i=1}^N w_i v_i$$



Fig. 12. DV\_mean detector: edges of the noised image 'Lena'



Fig. 13. DV\_alpha-trim detector: edges of the noised image 'Lena'



Fig. 14. DV\_adapt detector: edges of the noised image 'Lena'



# Difference vector iba v 2 smeroch

## horizontálne a vertikálne

$$DV_{hv} = \max(|\nabla f|_{0^\circ}, |\nabla f|_{90^\circ})$$

Ľudský vizuálny systém je viac citlivý na horizontálne a vertikálne hrany

časovo menej náročný

horizontálne a vertikálne rozdiely vo vektoroch prispievajú k detekcii diagonálnych hrán – detekované hrany sú tenšie



Fig. 16. DV\_hv<sub>mean</sub> detector: edges of the noised image 'Lena'



Fig. 15. DV\_hv detector: edges of the noised image 'Lena'

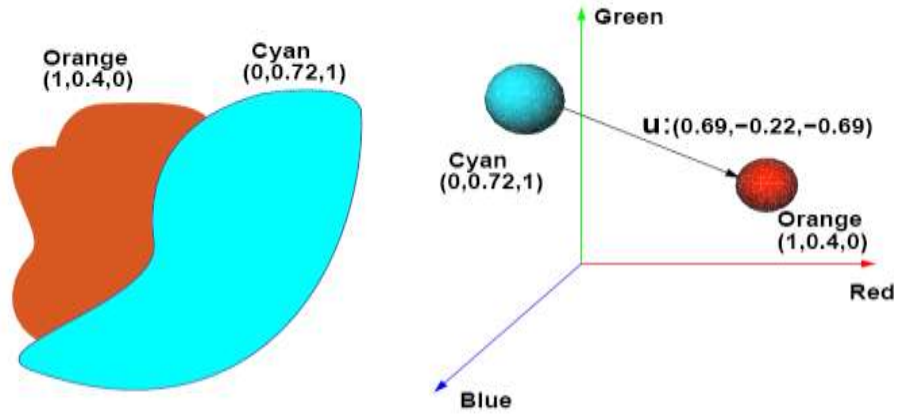
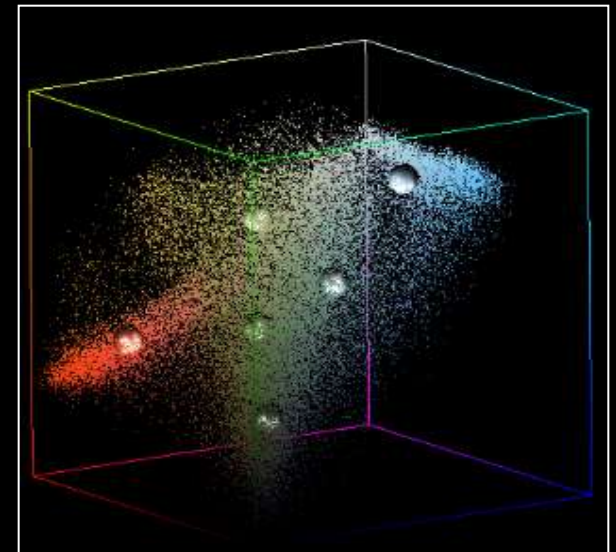


Fig. 17. DV\_hv <sub>$\alpha$ -trim</sub> detector: edges of the noised image 'Lena'



Fig. 18. DV\_hv<sub>adapt</sub> detector: edges of the noised image 'Lena'

# Detekcia hrán pomocou zgrupovania



(a)

(b)

Figure 1: (a) edge between two color regions (b)  $u$  - the best linear combination.



Sobel edge detection on gray  
Mandrill image



edge detected using proposed  
method resulted clusters

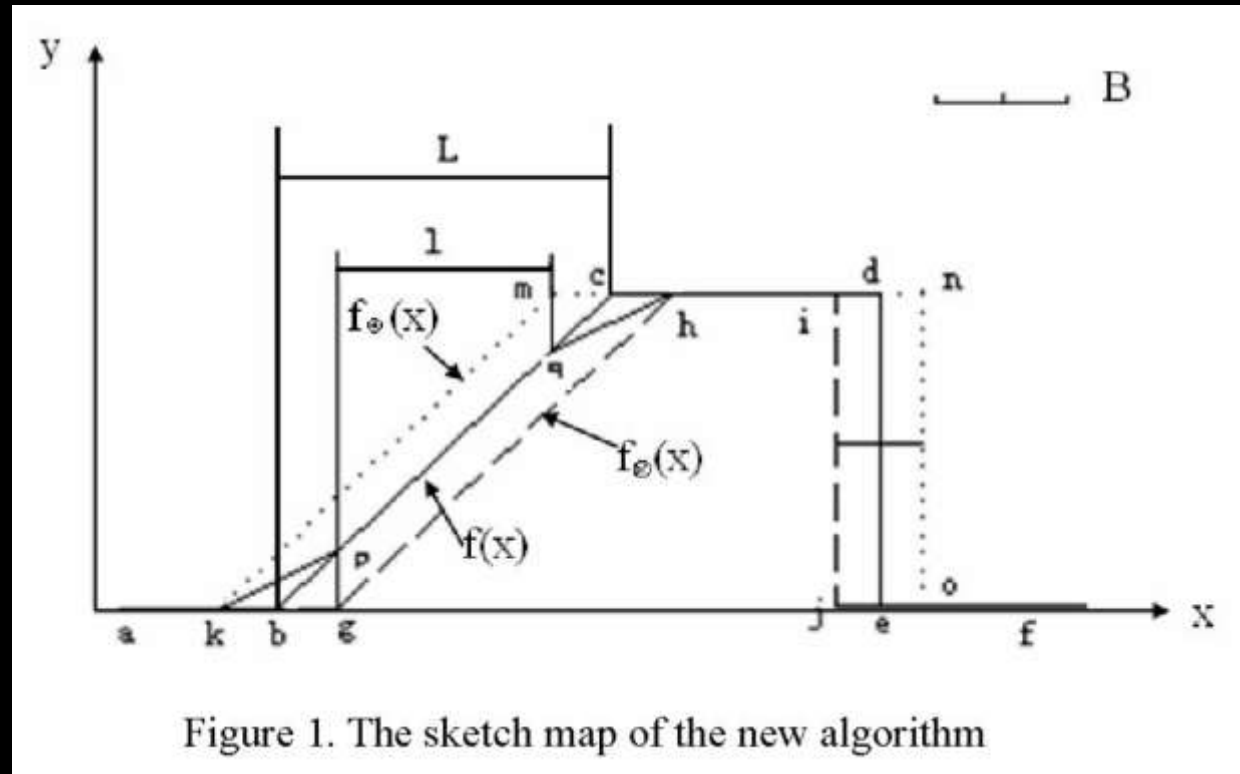
# Color Edge Detection Based on Morphology

bc, de – hrany  
 $f(x)$  – originálna funkcia

Erodovaný -  
 aghijf

Dilatovaný -  
 akmnof

Výsledný  $f'(x)$  -  
 agpqmdef



$$f'(x) = \begin{cases} f_{\oplus}(x) & \text{if } f(x) \geq (f_{\oplus}(x) + f_{\otimes}(x)) / 2 \\ f_{\otimes}(x) & \text{if } f(x) < (f_{\oplus}(x) + f_{\otimes}(x)) / 2 \end{cases}$$

# Color Edge Detection Based on Morphology

1. Erózia a dilatácia každého pixla na každom farebnom kanále
2. Vypočítaj  $f(x)$  2 krát
3. Vypočítaj gradient farebného obrazu
4. Detekcia hrán
5. Odstránenie šumových hranových bodov (izolovaný bod)

# Color Edge Detection Based on Morphology



Figure2. The origin color image

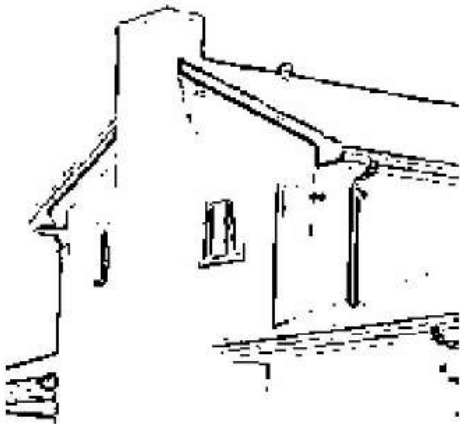


Figure 3. The edge image with Sobel operator

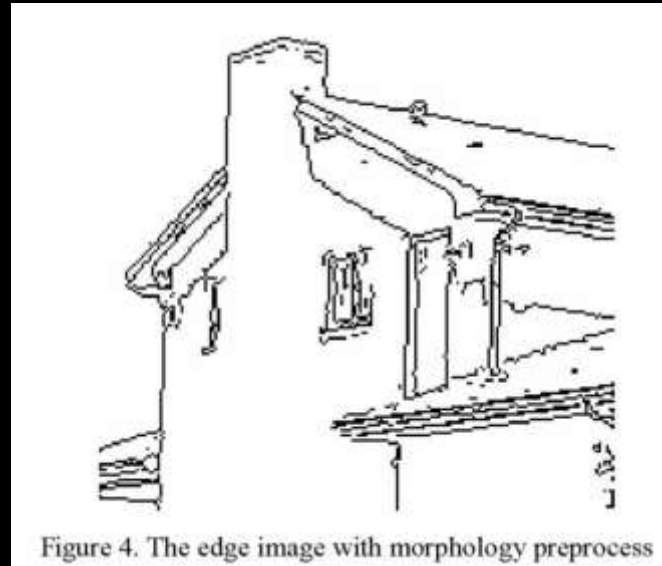


Figure 4. The edge image with morphology preprocess